# Description

# METHOD AND APPARATUS FOR GENERATING N-ORDER COMPENSATED TEMPERATURE INDEPENDENT REFERENCE VOLTAGE

### **BACKGROUND OF INVENTION**

- [0001] 1. Field of the Invention
- [0002] The invention relates to electronic circuits, and more particularly, to generating a constant reference voltage having N<sup>th</sup> order temperature compensation.
- [0003] 2. Description of the Prior Art
- Bandgap voltage reference circuits are widely used in various applications in order to provide a stable voltage reference over a temperature range. The bandgap voltage reference circuit operates on the principle of compensating the negative temperature coefficient of a base-emitter junction voltage,  $V_{BE}$ , with the positive temperature coefficient of the thermal voltage  $V_{T}$ , with  $V_{T}$  being equal to kT/

q. Typically, the variation of  $V_{BE}$  with temperature is approximately 1.5 mV/°C, while  $V_{T}$  is approximately +0.086 mV/°C. These terms are combined to generate the bandgap voltage,  $V_{RC}$ :

[0005]

$$V_{BG} = K_1 V_{BE} + K_2 V_T$$

Eq. (1)

[0006] where K<sub>1</sub> and K<sub>2</sub> are proportionality constants to ensure that the positive and negative thermal factors cancel one another, and, optionally, to scale the bandgap voltage to accommodate application requirements.

[0007] Fig.1 is a circuit diagram showing a typical bandgap voltage reference circuit 100. The bandgap voltage reference circuit 100 includes PMOS transistors M1, M2 and M3, bipolar transistors Q1 (having emitter area KA) and Q2 (having emitter area A), resistors R0, R1, R2 and R3, and an operational amplifier (Op-amp) 101. Please note that here, in Fig.1, the resistors R1 and R2 are of the same value. Transistors Q1 and Q2 conduct substantially equal currents. Because the ratio of the emitter areas of transistors Q1 and Q2 is K:1, a . V BE, of substantially V In(K), is produced across resistor R0, providing a proportional—to-absolute-temperature current. The Op-amp 101 forces

the voltages at nodes  $V_1$  and  $V_2$  to be equal, thereby causing currents to flow in resistors R1 and R2 which are proportional to  $V_{BE}$  and providing a complementary–to–absolute–temperature current. The resulting current through transistors M1 and M2 is thus compensated in accordance with Equation (1). The compensated current is mirrored to transistor M3 to generate the output voltage V.

OUT.

Specifically, in the bandgap reference circuit 100 of Fig.1, the output voltage  $V_{OUT}$  is defined by Equation (2):

[0009]

[8000]

$$V_{OUT} = \frac{R3}{R1} V_{BB2} + \frac{R3}{R0} V_T \ln(K),$$

Eq. (2)

[0010] where V<sub>BE2</sub> is the base-emitter voltage of transistor Q2 and K is the area ratio of transistors Q1 and Q2. Comparing Equation (2) with Equation (1), it is clear that the values of resistors R0, R1 and R3, and the emitter areas of transistors Q1 and Q2 are selected to provide the desired proportionality constants K<sub>1</sub> and K<sub>2</sub>. For any area ratio of transistors Q1 and Q2, it can be shown using Equation (2) that when the resistor values are selected to ensure the positive and negative thermal factors canceling one an-

- other, the bandgap reference circuit 100 generates a constant reference voltage  $V_{\rm OUT}$ .
- [0011] However, this constant reference voltage V<sub>OUT</sub> is only accurate at a specific center temperature. As the temperature of the bandgap reference circuit 100 deviates from the center temperature, there is a significant voltage change in the reference voltage V<sub>OUT</sub>. For example, over a temperature range from -40°C to +100°C, a voltage change of approximately 1mV is typical.

### **SUMMARY OF INVENTION**

- [0012] One objective of the claimed invention is therefore to provide an N<sup>th</sup> order compensated temperature independent voltage reference generator.
- [0013] According to embodiments of the present invention, a reference voltage generator having N<sup>th</sup> order temperature compensation is disclosed. The reference voltage generator comprises: a plurality of signal generators for producing a plurality of signals respectively corresponding to a plurality of temperature dependent characteristics; a combining module coupled to the signal generators for combining the plurality of signals to form a combined signal; and a signal to voltage converter coupled to the combining module for generating a compensated reference volt-

- age according to the combined signal.
- [0014] According to embodiments of the present invention, a method for generating a reference voltage having N<sup>th</sup> order temperature compensation is also disclosed. The method comprises: producing a plurality of signals respectively corresponding to a plurality of temperature dependent characteristics; combining the plurality of signals to form a combined signal; and generating a compensated reference voltage according to the combined signal.
- [0015] These and other objectives of the claimed invention will no doubt become obvious to those of ordinary skill in the art after reading the following detailed description of the embodiments that are illustrated in the various figures and drawings.

## **BRIEF DESCRIPTION OF DRAWINGS**

- [0016] Fig.1 is a circuit diagram showing a typical bandgap voltage reference circuit.
- [0017] Fig.2 shows a block diagram of a 2<sup>nd</sup> order compensated reference voltage generator according to an embodiment of the present invention.
- [0018] Fig.3 shows a first circuit diagram for a 2<sup>nd</sup> order compensated reference voltage generator according to a first embodiment of the present invention.

- [0019] Fig.4 shows a second circuit diagram for a 2<sup>nd</sup> order compensated reference voltage generator according to a second embodiment of the present invention.
- [0020] Fig.5 is a flowchart illustration a method of generating an N<sup>th</sup> order compensated reference voltage according to the present invention.

### **DETAILED DESCRIPTION**

- [0021] As temperature changes, the typical bandgap reference circuit 100 shown in Fig.1 has a variation in the output voltage V<sub>OUT</sub> primarily because the bandgap reference circuit 100 achieves only 1<sup>st</sup> order temperature compensation. The reason the bandgap reference circuit is only 1<sup>st</sup> order compensated for temperature is because only two base-emitter voltages (Q1 and Q2) are used.
- In order to produce a constant reference voltage having 2<sup>nd</sup> order compensation for temperature changes, at least three different temperature dependent characteristics, such as base-emitter voltages, need to be used. To explain 2<sup>nd</sup> order compensation, Equation (3) shows a Taylor series representation of the resultant output reference voltage V<sub>RFF</sub>.

$$\begin{split} V_{RBF} &= K_1 V_{BB1} + K_2 V_{BB2} + K_3 V_{BB3} \\ &= r_0 + r_1 (T - Tr) + r_2 (T - Tr)^2 + \dots \end{split}$$

Eq. (3)

[0024] Equation (4) shows an approximation that can be made

[0025] 
$$V_{RFF} \approx K_1(\beta_{1,0} + \beta_{2,0}(T - Tr) + \beta_{3,0}(T - Tr)^2 + ...)$$
  
  $+ K_2(\beta_{1,1} + \beta_{2,1}(T - Tr) + \beta_{3,1}(T - Tr)^2 + ...)$   
  $+ K_3(\beta_{1,2} + \beta_{2,2}(T - Tr) + \beta_{3,2}(T - Tr)^2 + ...)$ 

Eq. (4)

[0026] Therefore

$$r_{0} = K_{1}\beta_{1,0} + K_{2}\beta_{2,0} + K_{3}\beta_{3,0}$$

$$r_{1} = K_{1}\beta_{1,1} + K_{2}\beta_{2,1} + K_{3}\beta_{3,1}$$

$$r_{2} = K_{1}\beta_{1,2} + K_{2}\beta_{2,2} + K_{3}\beta_{3,2}$$

Eq. (5, 6, 7)

where, for  $2^{nd}$  order compensation,  $r_1$  and  $r_2$  are equal to zero. Generalizing for  $N^{th}$  order compensation, at least N+1 different temperature dependent characteristics, such as base-emitter voltages, need to be used, and  $r_1$  to

r, are equal to zero.

[0029] Fig.2 shows a block diagram of a 2<sup>nd</sup> order compensated reference voltage generator 200 according to an embodiment of the present invention. The 2<sup>nd</sup> order compensated reference voltage generator 200 includes a plurality of signal generators 202, a combining module 204, and a signal to voltage converter 206. The signal generators 202 respectively generate signals  $S_1$ ,  $S_2$ ,  $S_3$  corresponding to unique base-emitter junctions of bipolar junction transistors. As an example, in Fig.2, each signal generator 202 is shown having a current source  $I_1$ ,  $I_2$ ,  $I_3$ ; a base-emitter junction  $V_{BE1}$ ,  $V_{BE2}$ ,  $V_{BE3}$ ; and a scaling device for scaling the signal by a scaling factor  $K_1$ ,  $K_2$ ,  $K_3$ . The combining module receives the signals  $S_1$ ,  $S_2$ ,  $S_3$  and electrically adds or subtracts the signal  $S_1$ ,  $S_2$ ,  $S_3$  to form a combined signal S<sub>c</sub>. The signal to voltage converter generates a reference voltage  $V_{RFF}$  according to the combined signal  $S_{C}$ . By selecting appropriate scaling factors  $K_1$ ,  $K_2$ ,  $K_3$  to satisfy Equation (3) with  $r_1$  and  $r_2$  being equal to zero and the thermal factors (base-emitter voltages) canceling each other, the reference voltage  $V_{RFF}$  generated by the voltage generator 200 is a constant predetermined value having 2<sup>nd</sup> order compensation for temperature. Additionally, the

value  $V_{RFF}$  can be determined by the scale factors  $K_1$ ,  $K_2$ ,  $K_3$ 

[0030]

3, and a scale factor associated with the converter 206. Fig.3 shows a first circuit diagram for a 2<sup>nd</sup> order compensated reference voltage generator 300 according to a first embodiment of the present invention. The reference voltage generator 300 includes a first signal generator 302, a second signal generator 304, a third signal generator 306, a combining module 308, and a signal to voltage converter 310. The first signal generator 302 includes first and second PMOS transistors 312, 314, a resistor 316, a bipolar transistor 318, and an operational amplifier (op-amp) 320. The first and second PMOS transistors 312, 314 act as current sources and generate substantially equal currents I1 according to the output of the op-amp 320. The op-amp 320 ensures that the voltage at nodes A and B are equivalent. The voltage at nodes A and B is therefore the base-emitter voltage  $V_{RF}$  of the bipolar transistor 318 and depends on the emitter area of the bipolar transistor 318 and the current I1. By selecting the value of the resistor 316, the current  $I_1$  can be appropriately scaled. The output signal  $S_1$  of the first signal generator 302 is the output of the op-amp 320, which is effectively a control signal controlling the amount of current generated by the first and second PMOS transistors 312, 314. The second and third signal generators 304, 306 are structurally similar to the first signal generator, but have different bipolar transistor 324, 328 emitter areas and different resistor 322, 326 values, and, therefore, produce differently scaled output signals S2, S3, respectively.

[0031] The combining module 308 uses the signals S1, S2, S3 and a plurality of PMOS and NMOS transistors to reproduce the currents  $I_1$ ,  $I_2$ ,  $I_3$  from the first, second, and third signal generators 302, 304, 306, respectively. The three currents  $I_1$ ,  $I_2$ ,  $I_3$  are then combined such that  $S_C$  is equal to  $I_1$ ,  $I_3$ ,  $I_2$ . The signal to voltage converter 310 simply couples this combined current signal  $S_C$  outputted by the combining module 308 to ground using an output resistor 330. By selecting the emitter areas of the first, second, and third bipolar transistors 318, 324, 328 and the values of the resistors 316, 322, 326, 330, the value of  $V_{REF}$  can be fixed at a predetermined value independent of temperature having  $2^{nd}$  order temperature compensation.

[0032] Please note that, by observing the combining module 308 of this embodiment, the combining module 308 comprises a number of transistors, each of which respectively forms a current mirror configuration in conjunction with

transistors in each of the signal generators 302, 304, 306, through the communication of the signals S1, S2, S3. Although in this embodiment the currents generated by the transistors in the combining module 308 are respectively equal to those in the corresponding signal generators, it is well known that they can be scaled by properly designing the area ratio between the transistor in the combining module 308 and the transistor in the signal generator constituting a current mirror pair. Then such currents in the combining module 308 are combined, in this embodiment, using another current mirror. In other words, the combining module 308 arithmetically combines a plurality of currents according to the plurality of signals S1, S2, S3, to render the combined current signal S<sub>c</sub>.

In order to determine the specific resistor values, the following procedure can be used. First choose a ratio among the emitter areas of the three bipolar transistors 318, 324, 328. In the following example, assume the ratio among the emitter areas of the three bipolar transistors 318, 324, 328 is equal to 3:45:1, and the currents flowing through the transistors are the same. Next, use a simulation tool or experimental results to determine the dependence on temperature of the three emitter-base voltages V<sub>BE1</sub>, V<sub>BE2</sub>,

V<sub>BE3</sub> for the three bipolar transistors 318, 324, 328, respectively. For example, for a center temperature value T<sub>r</sub> of 40°C:

[0034] 
$$V_{BE1} = 748.6218 \ 1.7308(T - T_r) \ 0.0006(T - T_r)^2$$

[0035] 
$$V_{BE2} = 651.7201 \ 2.0533(T - T_r) \ 0.0007(T - T_r)^2$$

[0036] 
$$V_{BE3} = 760.4482 \ 1.6918(T - T_r) \ 0.0006(T - T_r)^2$$

Using Equation (8) shown below, the ratios between the resistance values  $R_1$ ,  $R_2$ ,  $R_3$ ,  $R_4$  of the resistors 316, 322, 326, 330 can be determined where  $r_1 = r_2 = 0$  for  $2^{nd}$  order temperature compensation.

$$\begin{split} V_{REF} &= K_1 V_{BE1} + K_2 V_{BE2} + K_3 V_{BE3} \\ &= R_4 \left( \frac{V_{BE1}}{R_1} - \frac{V_{BE3}}{R_3} - \frac{V_{BE2}}{R_2} \right) \\ &= r_0 + r_1 (T - Tr) + r_2 (T - Tr)^2 + \dots \end{split}$$

Eq. (8)

[0039] For low power consumption, large resistor values can be chosen. Continuing the above example, in order to generate a reference voltage at 700mV, after calculation, the following resistor values are determined:

[0040] First resistor 316 = 24.52 k

[0041] Second resistor 322 = 50 k

[0042] Third resistor 326 = 57.3 k

[0043] Output resistor 330 = 200 k

[0044] According this embodiment, the actual value of the reference voltage V<sub>REF</sub> is determined according to the scaling factors (resistors 316, 322, 326, 330) used in the signal generators 302, 304, 306 and the signal to voltage converter 310, respectively. In this way, reference voltage V<sub>REF</sub> with an even smaller value can be generated. The reference voltage V<sub>REF</sub> has N<sup>th</sup> order temperature compensation so is more accurate than the prior art 1<sup>st</sup> order bandgap reference circuit 100. Additionally, reference voltage V<sub>REF</sub> values lower than 1.2V can be generated, therefore, the present invention bandgap reference circuit can be used in very low supply-voltage circuits, for example, sub 1.5V power rail VDD applications.

Fig.4 shows a second circuit diagram for a 2<sup>nd</sup> order compensated reference voltage generator 400 according to a second embodiment of the present invention. The reference voltage generator 400 shown in Fig.4 includes similar components as the reference voltage generator 300 shown in Fig.3; however, the reference voltage generator

400 shown in Fig.4 includes first and second signals generators being merged together labeled 402. More specifically, the first signal generator includes a first PMOS transistor 404, a second PMOS transistor 406, a first resistor 408, a first bipolar transistor 410, and a first op-amp 412; and the second signal generator includes a third PMOS transistor 414, the second PMOS transistor 406, a second resistor 416, a second op-amp 415, the first bipolar transistor 410, and a second bipolar transistor 418. The components making up the first signal generator are connected in similar way as in Fig. 3. The components making up the second signal generator are similarly connected, except the second resistor 416 is connected to the emitter of the second bipolar transistor 418, which has its base and collector both tied to ground. In this way the first signal generator and the second signal generator share the second PMOS transistor 406 and the first bipolar transistor 410. Additionally, by connecting the second resistor 416 to a reference voltage being the emitter of the second bipolar transistor 418, which is at the baseemitter voltage  $V_{RF}$  for the second bipolar transistor 418, it becomes easier to calculate the values for the resistors 408, 416, 420 in the signal generators 402, 424, and the

output resistor 426 in the signal to voltage converter 428. In Fig.4, the operation of the 2<sup>nd</sup> order compensated reference voltage generator 400 is otherwise the same as described for Fig.3.

[0046] Although pnp bipolar transistors have been used in the previous examples and diagrams, the present invention is not limited to pnp transistors, and it is possible to use npn transistors while still following the teachings of the present invention. Additionally, other temperature dependent characteristics, such as the current through a diode being dependent on the thermal voltage V<sub>T</sub> (dependent on temperature), can be used with the present invention. In general, by using N different devices, each device having a different temperature dependent characteristic, compensation to the (N-1)<sup>th</sup> order can be achieved.

[0047] As such, Fig.5 is a flowchart illustrating a method of generating an N<sup>th</sup> order temperature compensated reference voltage according to an embodiment of the present invention. The flowchart in Fig.5 contains the following steps:

[0048] Step 500:Produce N+1 signals being dependent on temperature. These signals can be produced according to N+1 base-emitter voltages of N+1 different bipolar transistors, or other temperature dependent characteristics.

- [0049] Step 502:Combine the N+1 signals to form a combined signal. When combined, the N+1 signals must satisfy Equation (8), where r1 to r<sub>N</sub> are set to zero to achieve N<sup>th</sup> order compensation. In this way the thermal factors of the N+1 signals cancel out.
- [0050] Step 504:Generate  $V_{REF}$  according to the combined signal formed in Step 502.
- [0051] According to the embodiments of the present invention, the value of the reference voltage V<sub>REF</sub> is determined according to the resistors used in the signal generators and the signal to voltage converter. In this way, reference voltage V<sub>REF</sub> feasible for low voltage applications, for example, sub 1.5V applications, can be generated. The present invention is therefore suitable for use in very low supplyvoltage VDD circuits and produces a constant reference voltage having N<sup>th</sup> order temperature compensation.
- [0052] Those skilled in the art will readily observe that numerous modifications and alterations of the device may be made while retaining the teachings of the invention. Accordingly, the above disclosure should be construed as limited only by the metes and bounds of the appended claims.